DYNAMICS OF TURBULENT TRANSPORT IN TOKAMAKS AND STELLARATORS





RES Scientific Seminar 2014: Engineering October 15, 2014, Barcelona, SPAIN



David Newman, University of Alaska at Fairbanks, USA Viktor Decyk and Jean-Noel Leboeuf*, UCLA, USA Luis García, José M. Reynolds, Jorge Alcusón, Universidad Carlos III de Madrid Ben Carreras* and Vickie Lynch, Oak Ridge National Laboratory, USA Pavlos Xanthopoulos, IPP-Max Planck Institute, Greifswald, GERMANY



(*)retired

PLASMAS

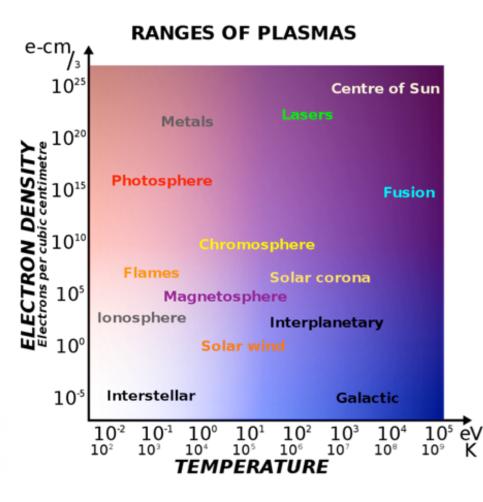
Plasma is loosely described as an electrically neutral medium of positive and negative particles.

Although particles are unbound, they <u>are not</u> <u>'free'</u>. When the charges move they generate electrical currents with magnetic fields, and as a result, they are affected by each other's fields. These nonlinear interactions govern their collective behavior with many degrees of freedom.

PLASMA TURBULENCE

Characteristic	Typical ranges of plasma parameters: orders of magnitude	
	Terrestrial plasmas	Cosmic plasmas
Size in meters	10 ⁻⁶ m (lab plasmas) to 10 ² m (lightning) (~8 OOM)	10 ⁻⁶ m (spacecraft sheath) to 10 ²⁵ m (intergalactic nebula) (~31 OOM)
Lifetime in seconds	10 ⁻¹² s (laser-produced plasma) to 10 ⁷ s (fluorescent lights) (~19 OOM)	10 ¹ s (solar flares) to 10 ¹⁷ s (intergalactic plasma) (~16 OOM)
Density in particles per cubic meter	10 ⁷ m ⁻³ to 10 ³² m ⁻³ (inertial confinement plasma)	1 m ⁻³ (intergalactic medium) to 10 ³⁰ m ⁻³ (stellar core)
Temperature in kelvins	~0 K (crystalline non-neutral plasma ^[12]) to 10 ⁸ K (magnetic fusion plasma)	10 ² K (aurora) to 10 ⁷ K (solar core)
Magnetic fields in teslas	10 ⁻⁴ T (lab plasma) to 10 ³ T (pulsed-power plasma)	10 ⁻¹² T (intergalactic medium) to 10 ¹¹ T (near neutron stars)

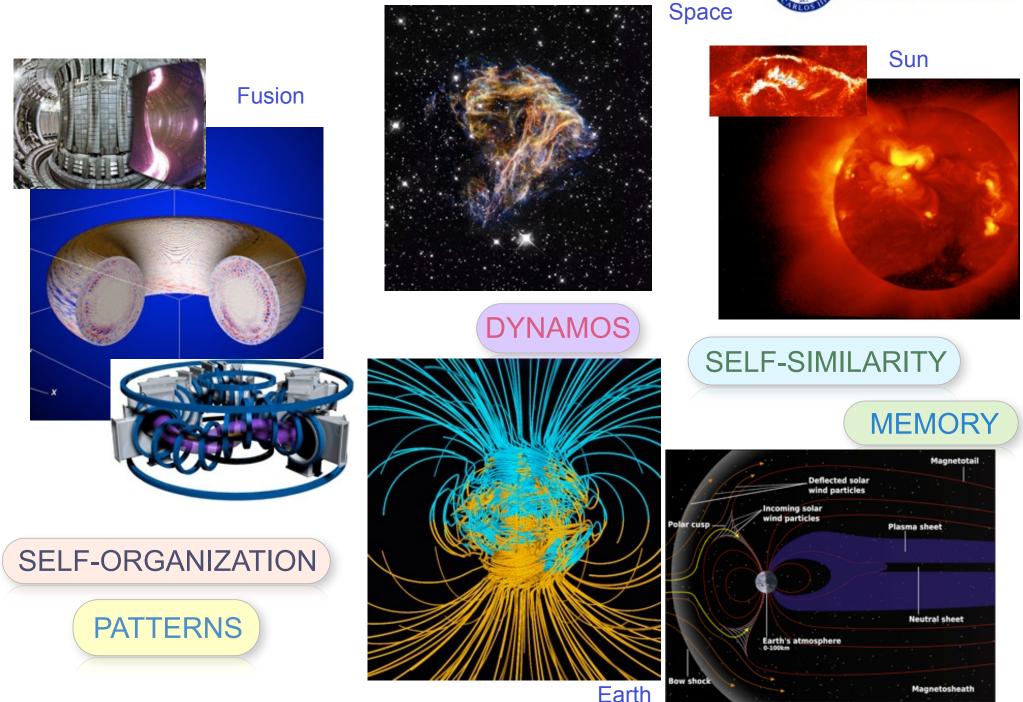




TURBULENCE IN PLASMAS



Universidad Carlos III de Madrid

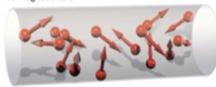


FUSION ENERGY: ITER and beyond

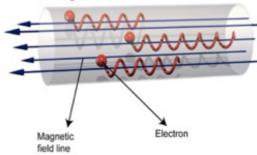


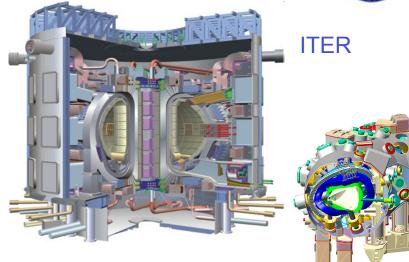
Universidad Carlos III de Madrid

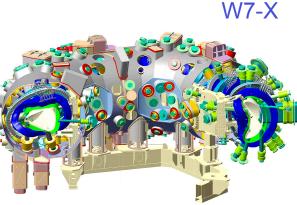
No magnetic field



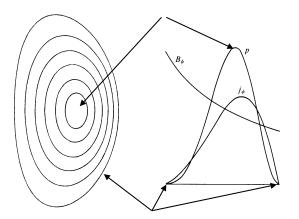
With magnetic field

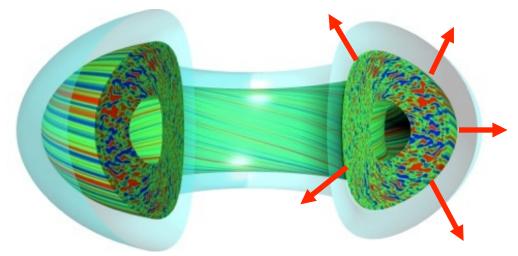






Helical magnetic fields can be used to confine hot plasmas long enough to produce energy





GYRO. General Atomics

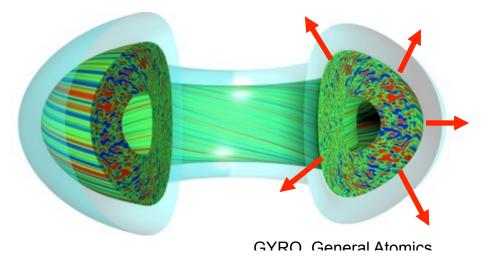
Turbulence dominates radial losses of energy and particles

MOTIVATION



Universidad Carlos III de Madrid

FACT: Turbulence dominates radial transport in tokamaks and stellarators. Thus, it determines how large a device must be to produce energy by fusion in an economically attractive way.



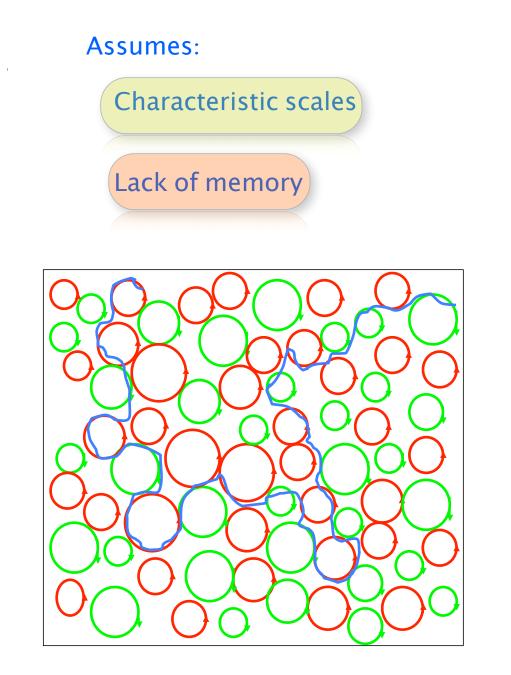
FACT: Traditionally, one simply estimates effective transport coefficients that encapsulate the overall effect of turbulence on confinement, while ignoring the smaller/shorter scale physics of turbulence.

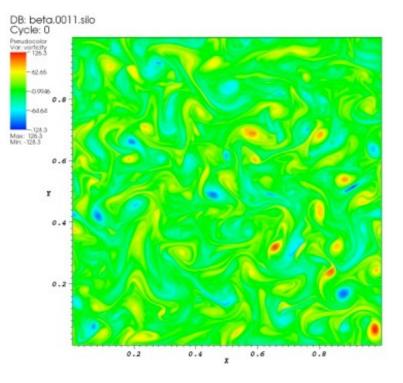
FACT: Most first-principle turbulent simulations are run for short periods of time, assuming that profile modification (i.e., transport) is irrelevant to calculate these coefficients.

Engineering QUESTION: is this the optimal way to design a reactor? Physics QUESTION: do we really understand what is going on?

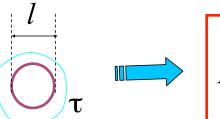
EFFECTIVE TURBULENT DIFFUSION: when does it work?

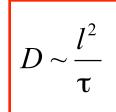






user: newman Thu Apr 12 22:00:45 2007





EFFECTIVE TURBULENT DIFFUSION: mathematical assumptions



[See: R. Balescu, "Aspects of Plasma Turbulent Transport", IOP, Bristol (2005)]

$$\frac{\partial n}{\partial t} + (\mathbf{V} \cdot \nabla) n = 0$$

$$\frac{\partial n_0}{\partial t} = -\left\langle \tilde{\mathbf{V}} \cdot \nabla \tilde{n} \right\rangle$$

$$\frac{\partial \tilde{n}}{\partial t} + \tilde{\mathbf{V}} \cdot \nabla \tilde{n} = -\tilde{\mathbf{V}} \cdot \nabla n_0 + \left\langle \tilde{\mathbf{V}} \cdot \nabla \tilde{n} \right\rangle$$

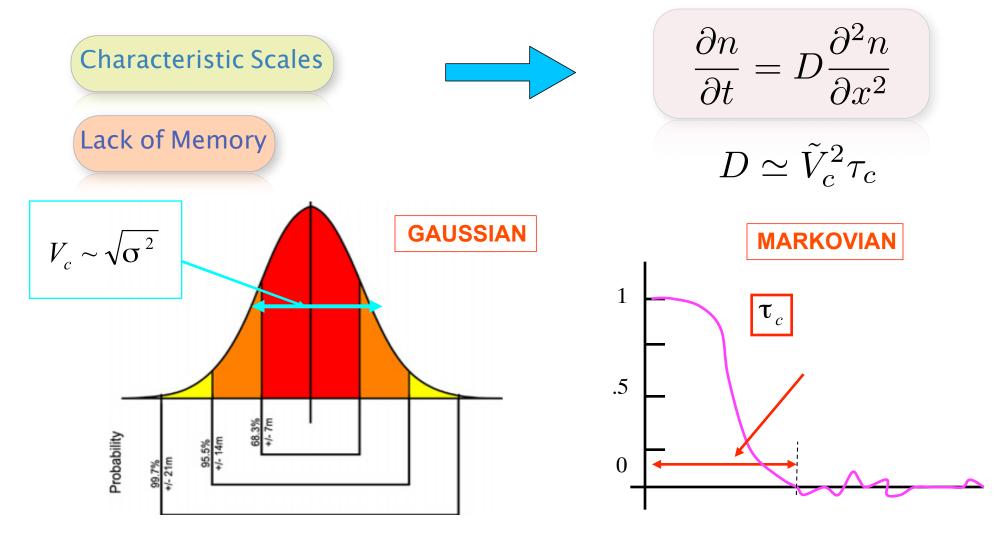
$$\frac{\partial n_0}{\partial t} = \nabla \cdot \int_0^t \left\langle \tilde{\mathbf{V}}(\mathbf{r}, t) \tilde{\mathbf{V}}(\mathbf{R}(t' | \mathbf{r}, t), t) \nabla n_0(\mathbf{R}(t' | \mathbf{r}, t), t) \right\rangle$$

$$\frac{\partial n_0}{\partial t} = \tilde{\mathbf{V}}(\mathbf{R}, \tau), \quad \mathbf{R}(t) = \mathbf{r}$$

REDUCTION TO DIFFUSIVE DESCRIPTION: Lagrangian view



$$\frac{\partial n_0}{\partial t} = \nabla \cdot \int_0^t \left\langle \tilde{\mathbf{V}}(\mathbf{r}, t) \tilde{\mathbf{V}}(\mathbf{R}(t'|\mathbf{r}, t), t) \nabla n_0(\mathbf{R}(t'|\mathbf{r}, t), t) \right\rangle$$



Transport scales are not necessarily turbulent decorrelation scales!



Radial Direction

[See: G.R. McKee et al, IEEE Tran. Plasma Sci. (2002)]

From point (<u>Eulerian</u>) probe data, both a finite decorrelation length (i.e., typical length scale) and a finite decorrelation time (i.e., typical time scale and thus no long– term memory) are obtained for turbulence.

But are turbulent decorrelation scales the ones characteristic of the transport process?

Apparently not always.

Two cases have been identified:

Near-marginal turbulence With strong sheared flows present

Poloidal Direction $t = 0 \mu s$ +10 µs +20 µs

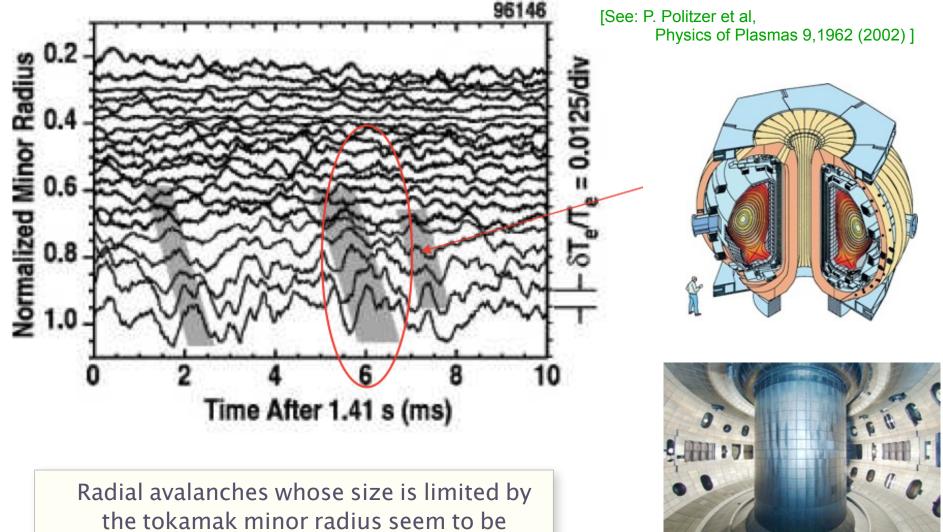
Fig. 1. Images of density fluctuations at $10 \cdot \mu s$ intervals, obtained over a 5-cm (radial) \times 6-cm (poloidal) region at the outer plasma midplane, $\rho = 0.9-1.05$, in a low-confinement (*L*-mode) discharge. White arrows in (a) qualitatively indicate average flow direction and magnitude.

102084, 850 mi

Both relevant in reactor conditions!

Is there any evidence from the experiments?

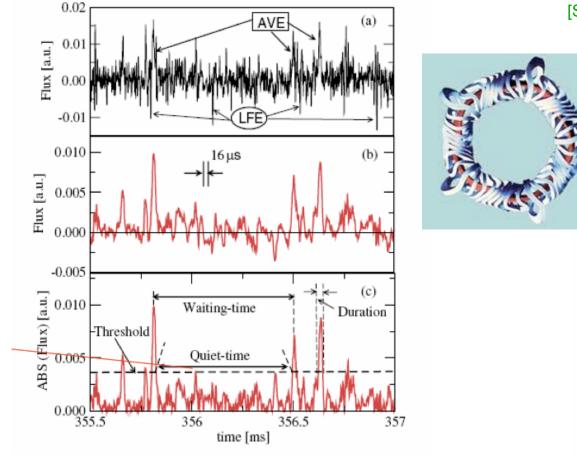


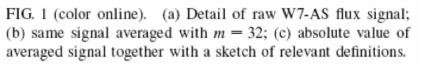


present in the ECE diagnostic?

Is there any evidence from the experiments?







Temporal correlations beyond local turbulent timescales seem apparent in Langmuir probe data.

[See: R. Sanchez, B.Ph. van Milligen, et al, Physical Review Letters 90,185005 (2003)]

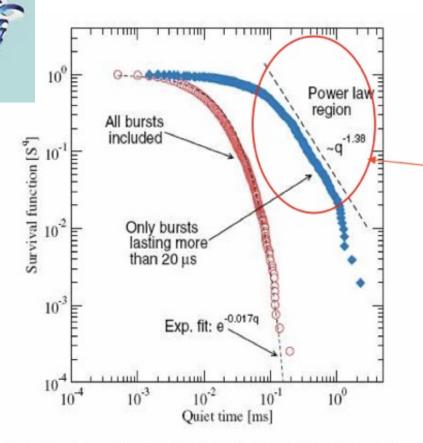


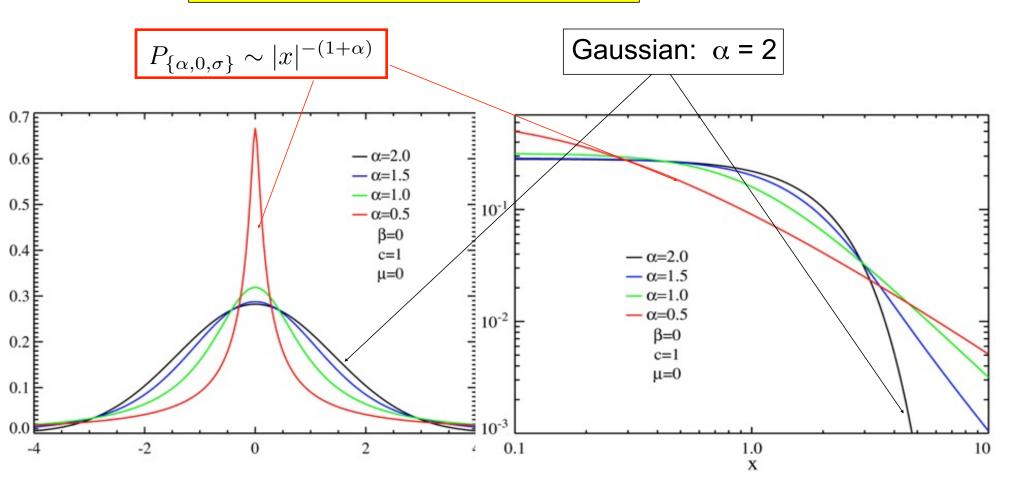
FIG. 2 (color online). Examples of quiet-time survival functions for W7-AS shot No. 35427.



$$\frac{\partial n_0}{\partial t} = \nabla \cdot \int_0^t \left\langle \tilde{\mathbf{V}}(\mathbf{r}, t) \tilde{\mathbf{V}}(\mathbf{R}(t'|\mathbf{r}, t), t) \nabla n_0(\mathbf{R}(t'|\mathbf{r}, t), t) \right\rangle$$

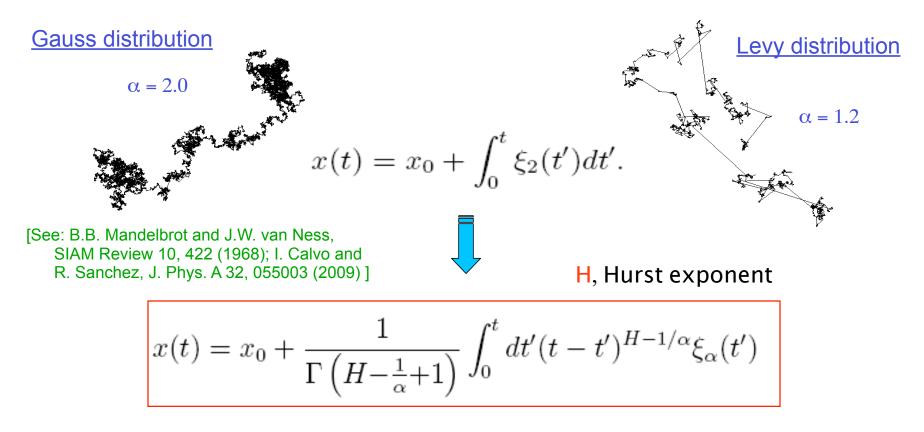
 $\implies P_{\{\alpha,0,\sigma\}} \sim |x|^{-(1+\alpha)}(k) = \exp(-\sigma^{\alpha}|k|^{\alpha}), \quad \alpha \le 2$

[See: G. Samorodnitsky and M. Taqqu, "Stable non-Gaussian distributions", Chapman and Hall, New York (1994)]





$$\frac{\partial n_0}{\partial t} = \nabla \cdot \int_0^t \left\langle \tilde{\mathbf{V}}(\mathbf{r}, t) \tilde{\mathbf{V}}(\mathbf{R}(t'|\mathbf{r}, t), t) \nabla n_0(\mathbf{R}(t'|\mathbf{r}, t), t) \right\rangle$$

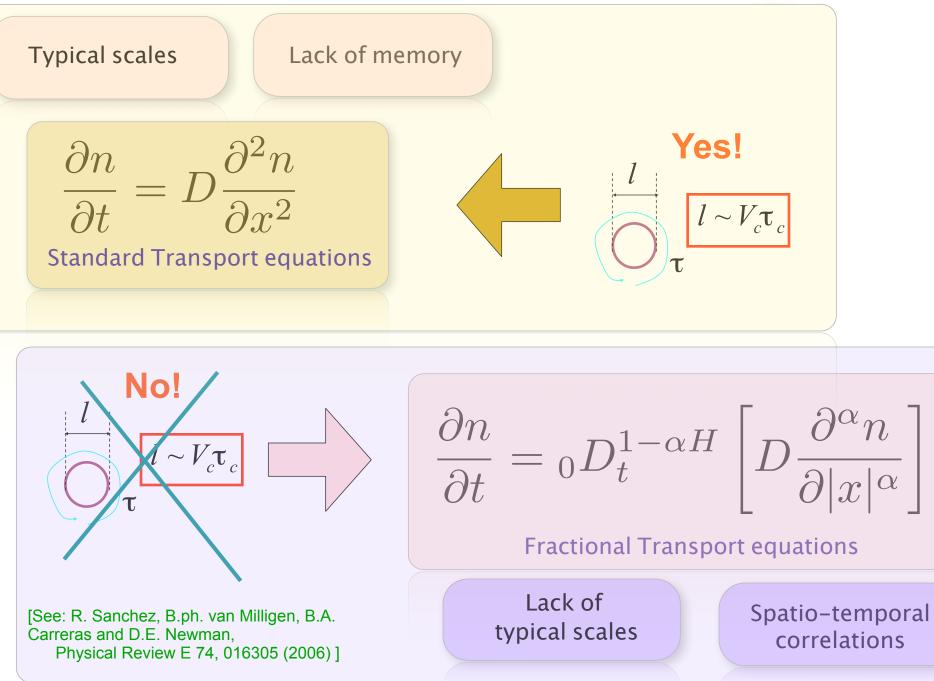


H=1/α, random; $H > 1/\alpha$, correlated positively; $H < 1/\alpha$, correlated negatively [See: H.E. Hurst, Trans. Am. Soc. Civ. Eng. 110, 770 (1951)]]

"Complex" EFFECTIVE TRANSPORT

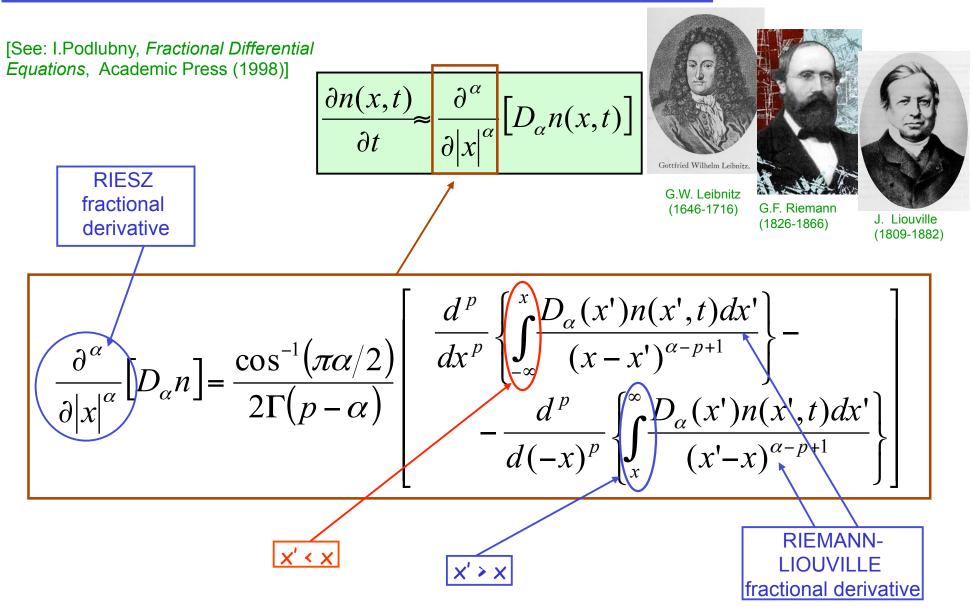


Universidad Carlos III de Madrid



SPATIAL FRACTIONAL DERIVATIVES: NONLOCAL OPERATORS





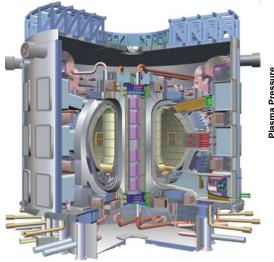
TURBULENT TRANSPORT ACROSS STABLE SHEARED FLOWS

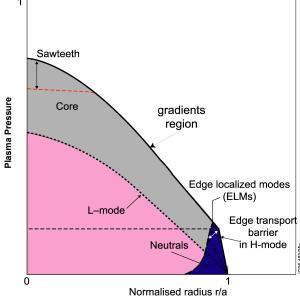
The appearance of stable sheared flows driven by turbulence is an example of self-organization and emergence of complex dynamics in many systems.

In plasmas, (mostly) poloidal flows with radial shear appear naturally at the plasma edge beyond a certain threshold power.

These flows allow access to enhance confinement regimes (H-mode). ITER will operate in this regime.

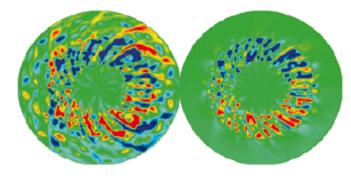
ITER tokamak, CEA, France





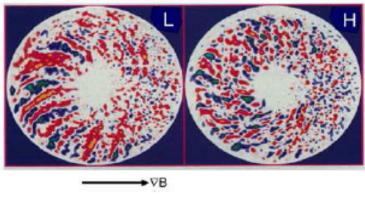
Universidad Carlos III de Madrid

Fluid resistive interchange turbulence (cylinder)



[See: B.A. Carreras et al, Phys. Fluids B 5 (1993) 1491]

Toroidal ITG gyro-kinetic simulations



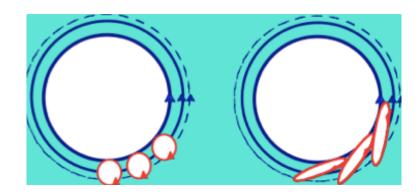
[See: Z. Lin et al, Science 281 (1998) 1835]

REDUCTION OF TURBULENT TRANSPORT ACROSS RADIALLY-SHEARED POLOIDAL FLOWS

> ITER and other devices rely on sheared flows to tame turbulence and access enhanced confinement regimes







Can reduced transport coefficients describe this process?

NATURE OF TURBULENT TRANSPORT ACROSS RADIALLY-SHEARED POLOIDAL FLOWS



Universidad Carlos III de Madrid

Ion-temperature-gradient (ITG) turbulence simulations realized with the UCAN code.

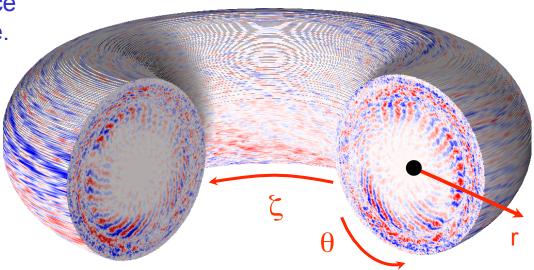
UCAN characteristics:

- δf -method
- Particle-in-Cell (PIC)
- kinetic ions, adiabatic electrons
- global, toroidal geometry
- collisionless
- electrostatic
- low- β

[See: R. Sydora et al, Pl. Phys. Contr. Fusion 38, A281 (1996)]

RUN parameters:

- 512x512x256 ions
- 256x256x128 spatial grid points
- 8 particles/cell



PHYSICAL PARAMETERS (DIIID-like):

- Central ion/electron temp [Kev]: 0.68/0.68
- Magnetic field [T]: 1.8
- Axis density [x10²⁰m⁻³]: 0.2
- Major/minor radius [m]: 2.5/0.56
- Ion Larmor radius [mm]: 2.85
- Temporal length of simulation [ms]: 5.56

Most of the results shown have been obtained at the AMD-Penguin Computing Cluster 'Pacman' at the Arctic Region Supercomputer Center in Alaska, as well as the IBM iDataPlex with Intel Sandy Bridge processors 'Mare Nostrum III' at the Barcelona Supercomputer Center in Spain.



Ion distribution function equation

$$\frac{\partial \delta f}{\partial t} + \frac{d\vec{R}}{dt} \cdot \vec{\nabla} \delta f + \frac{dv_{\parallel}}{dt} \frac{\partial \delta f}{\partial v_{\parallel}} = -\frac{d\vec{R}^{(1)}}{dt} \cdot \vec{\nabla} f_{0} - \frac{dv_{\parallel}^{(1)}}{dt} \frac{\partial f_{0}}{\partial v_{\parallel}} \qquad f = f_{0} + \delta f \qquad (2.1)$$

$$\frac{\partial \mathbf{w}}{\partial t} = -(1-\mathbf{w})\left[\frac{d\vec{R}^{(1)}}{dt}\cdot\vec{\nabla}f_0 + \frac{d\mathbf{v}_1^{(1)}}{dt}\frac{1}{f_0}\frac{\partial f_0}{\partial \mathbf{v}_1}\right] \qquad \mathbf{w} = \frac{\delta f}{f}$$
(2.2)

1

Method of characteristics: follow ion markers in phase space

$$\frac{d\vec{R}}{dt} = v_1\hat{b} + \vec{v}_E + \frac{c}{qB}\mu\hat{b}\times\vec{\nabla}B + \frac{v_1^2}{\Omega}\hat{b}\times(\hat{b}\cdot\nabla)\hat{b} \qquad \rho_i = \frac{v_\perp}{\Omega} \quad \mu = \frac{Mv_\perp^2}{2B} \quad \Omega = \frac{qB}{Mc} \quad (2.5)$$
$$\frac{dv_1}{dt} = \frac{q}{M}E_1 - \frac{1}{M}\mu(\hat{b}\cdot\vec{\nabla}B) \qquad (2.6)$$

Poisson equation: electrostatic potential

$$\frac{1}{\lambda_{Di}^{2}}\phi[1-\Gamma_{0}(k_{\perp}^{2}\rho_{i}^{2})] = 4\pi |e|(n_{i}-n_{e}) \qquad \lambda_{Di}^{2} = \frac{T_{i}}{4\pi n_{0}e^{2}} \qquad (2.7)$$

$$n_{i} = \oint \frac{d\varphi}{2\pi} N_{i} (\vec{R} + \rho_{i})$$

$$n_{e} = n_{0} \frac{|e|}{T_{e}} [\phi - \langle \phi \rangle]$$
(2.8)
(2.9)

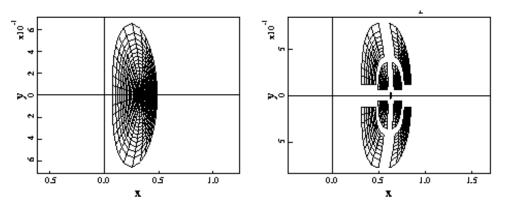
UCAN parallelizes spatially, not over particles.

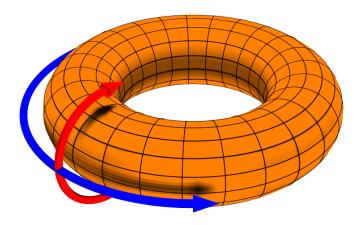
First version, UCAN, only parallelized toroidally, so that each processor handled a toroidal section.

UCAN2 applies domain decomposition techniques to each toroidal section, that can be now divided among processors

Marker ions are passed from one processor to another, as they exit the spatial region controlled by the first processor and enter the region controlled by the second processor

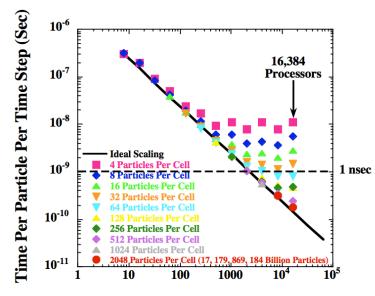
Communication happens mostly whenever particles change spatial domains, or when Poisson solves are done.







UCAN2 Parallel Scaling Studies



Number of Processors

Fig. 4: Time per particle per time step versus number of processors for a system size of 256 x 256 x 128 and from 4 to 2048 particles per cell for a maximum of 17,169,869,184 particles.

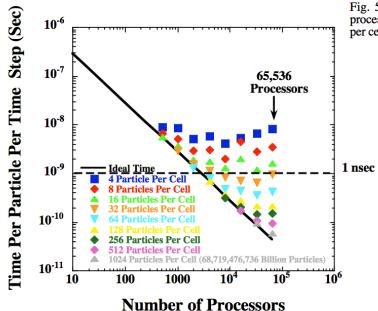
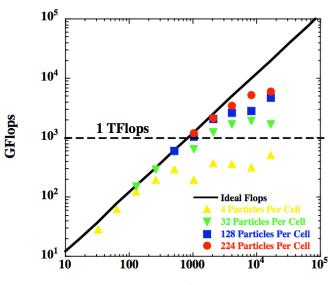


Fig. 6: Time per particle per time step in seconds versus number of processors up to 65,536 processors. The system size for these calculations is $512 \times 512 \times 256$ with 4 up to 1024 particles per cell for a maximum of 68,719,476,736 particles.





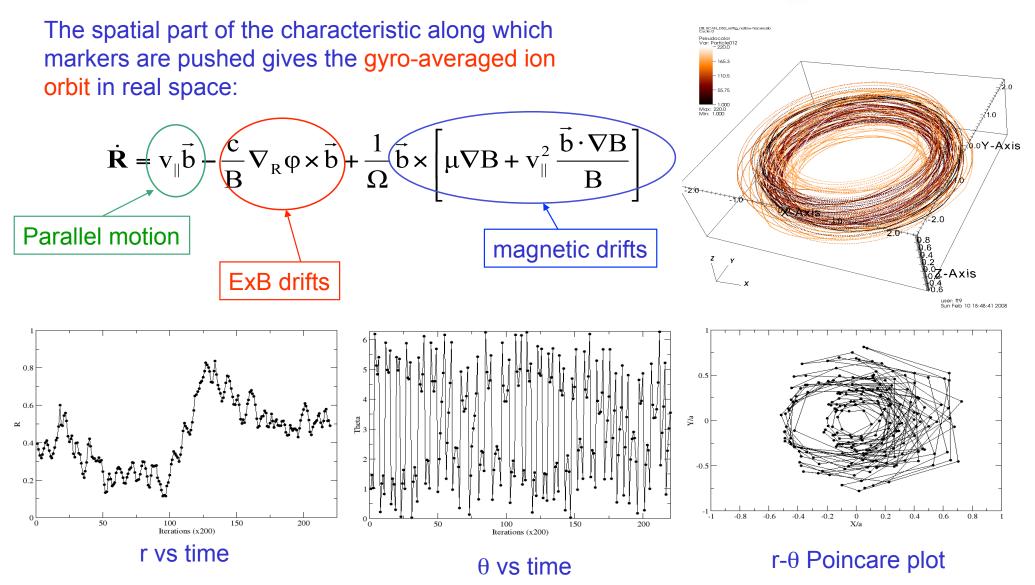
Number of Processors

Fig. 5: Floating point operations per second in GFlops versus number of processors for a system size of $256 \times 256 \times 128$ and from 4 to 224 particles per cell for a maximum of 2,046,820,352 particles.

Scaling results have been obtained mostly on the Cray XC30 'Edison' at NERSC, but also on the Cray XE6 and the IBM iDataPlex at NERSC, as well as the IBM iDataPlex with Intel Sandy Bridge processors 'Mare Nostrum III' at the Barcelona Supercomputer Center in Spain.

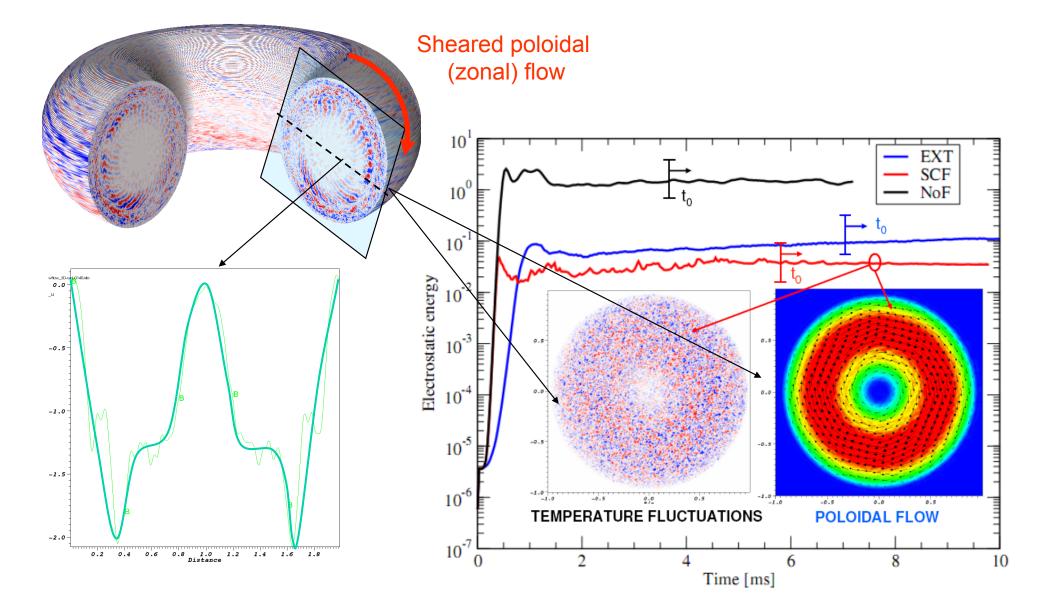
Ion trajectories









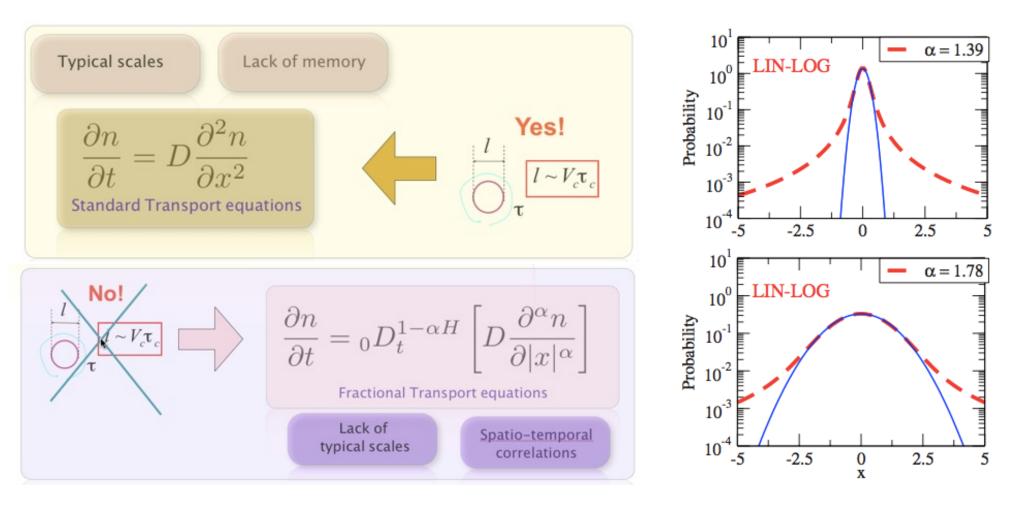


PROPAGATORS AS DIAGNOSTICS



Propagators are the solutions of any differential equation starting from a δ -function initial condition.

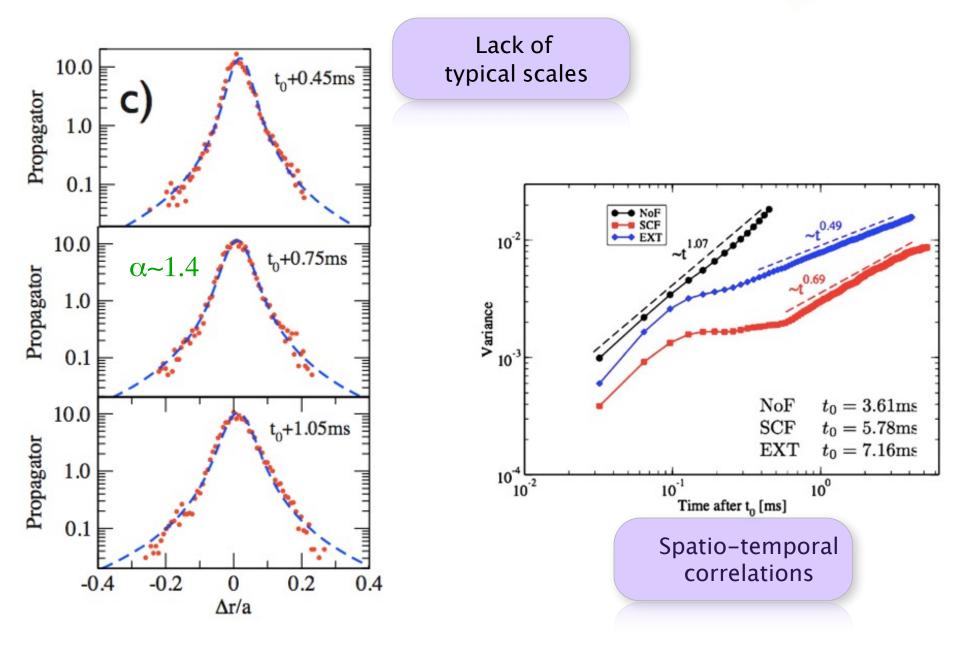
Propagators are very easy to construct numerically by using particles/tracers/ markers. Comparison with analytic expressions may yield transport exponents.



COMPLEX CROSS-FLOW TRANSPORT

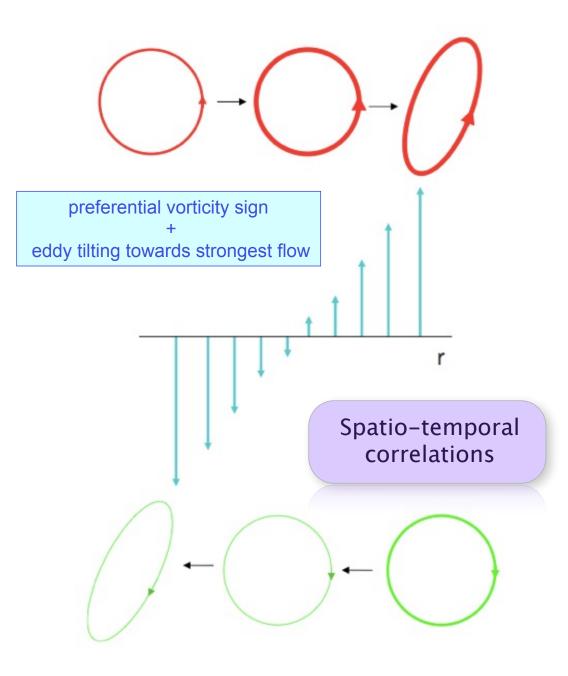


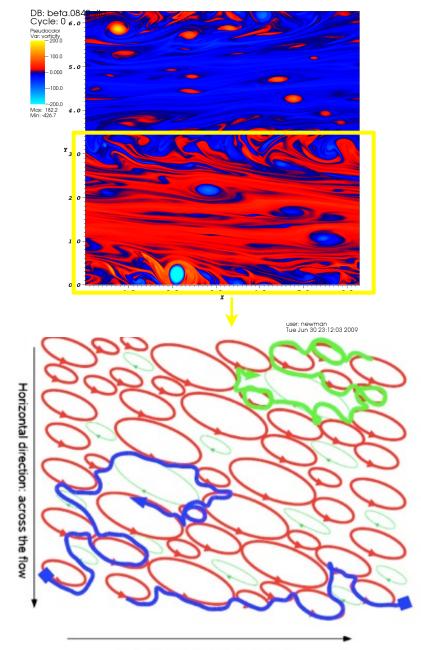
Universidad Carlos III de Madrid



PHYSICS OF SUBDIFFUSION



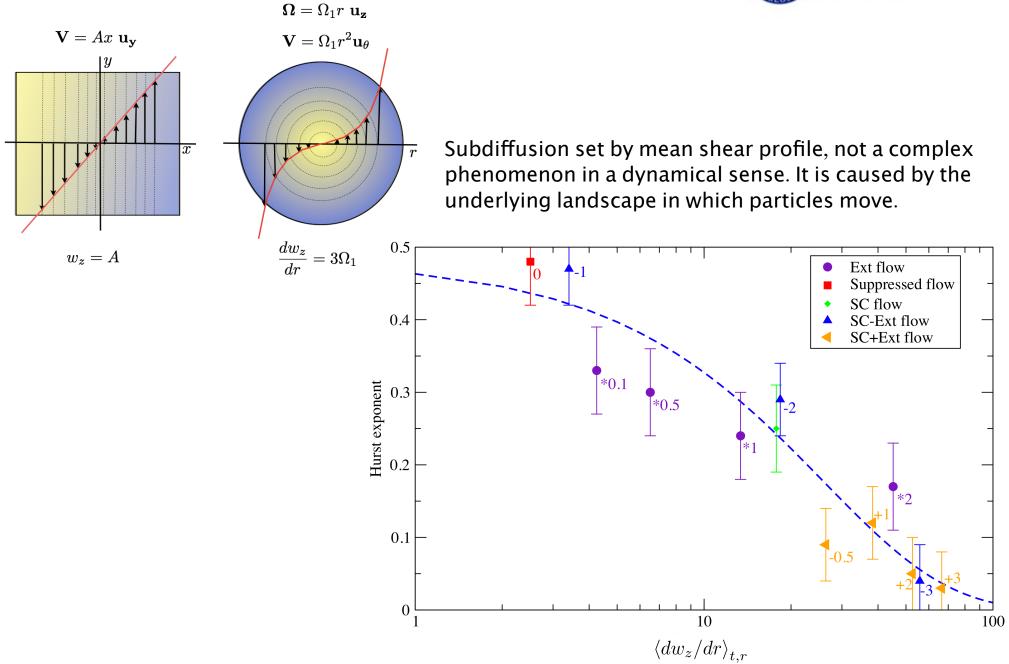




Vertical direction: along the flow

PHYSICS OF SUBDIFFUSION

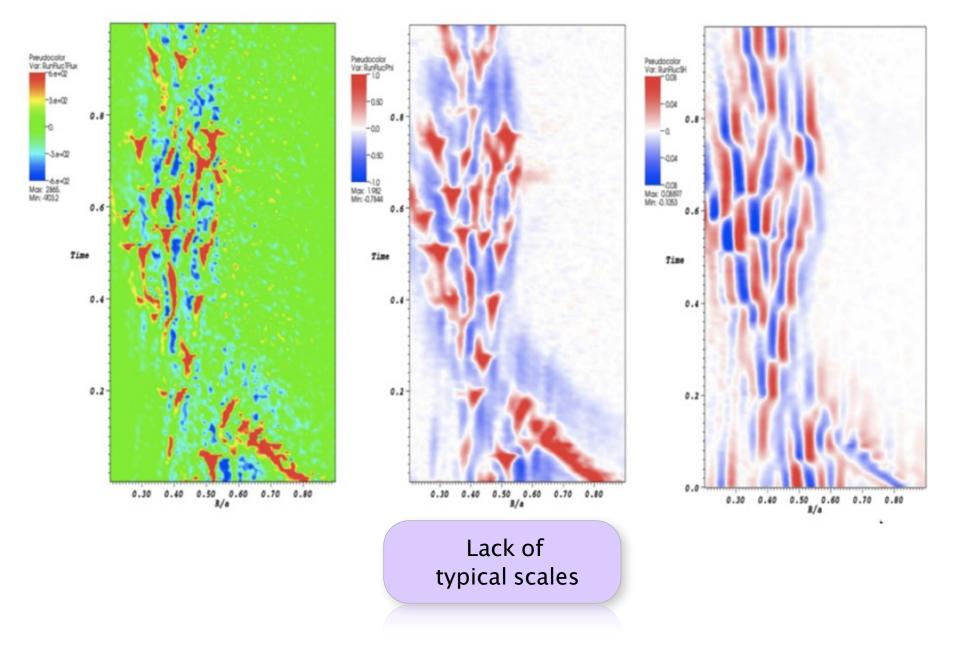




PHYSICS OF NON-GAUSSIANITY



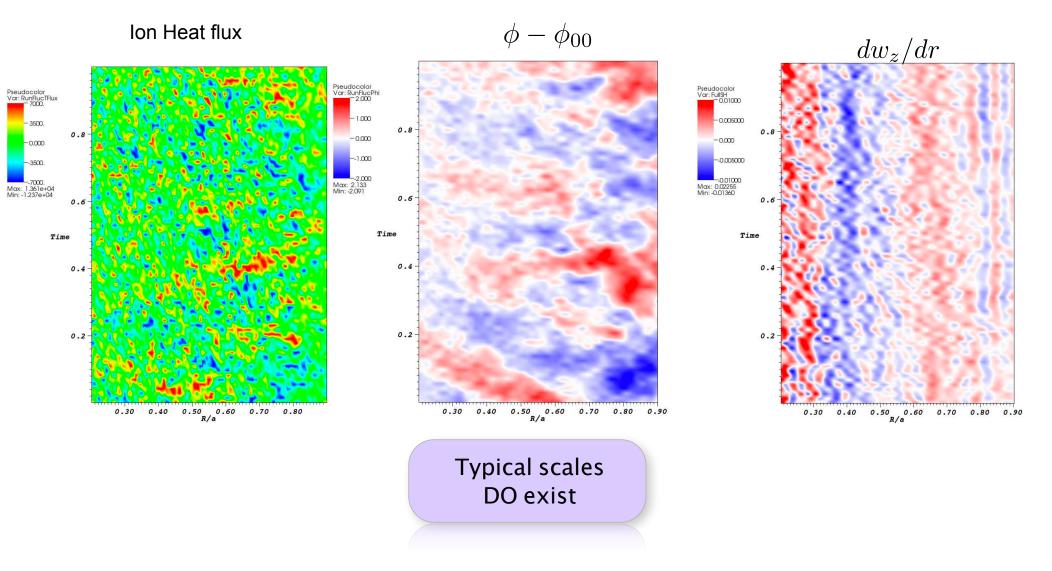
Predator-prey dynamics between fluctuations of turbulence and fluctuations in the shear of the flow



PHYSICS OF NON-GAUSSIANITY (II)



Effective diffusion provides good description when coupling between zonal flow and fluctuations <u>artificially suppressed</u>.



Publications

PRL 101, 205002 (2008)

PHYSICAL REVIEW LETTERS

week ending 14 NOVEMBER 2008

Nature of Transport across Sheared Zonal Flows in Electrostatic Ion-Temperature-Gradient Gyrokinetic Plasma Turbulence

 R. Sánchez, ^{1,*} D. E. Newman,² J.-N. Leboeuf,³ V. K. Decyk,⁴ and B. A. Carreras⁵
 ¹Fusion Energy Division, Oak Ridge National Laboratory, Oak Ridge, Tennessee 37831-8071, USA
 ²Department of Physics, University of Alaska, Fairbanks, Alaska 99775-5920, USA
 ³JNL Scientific Inc., Casa Grande, Arizona 85294-9695, USA
 ⁴UCLA, Los Angeles, California 90095-1547, USA
 ⁵BACV Solutions Inc., Oak Ridge, Tennessee 37830-8222, USA (Received 6 May 2008; published 12 November 2008)

It is shown that the usual picture for the suppression of turbulent transport across a stable sheared flow based on a reduction of diffusive transport coefficients is, by itself, incomplete. By means of toroidal gyrokinetic simulations of electrostatic, collisionless ion-temperature-gradient turbulence, it is found that the nature of the transport is altered fundamentally, changing from diffusive to anticorrelated and subdiffusive. Additionally, whenever the flows are self-consistently driven by turbulence, the transport gains an additional non-Gaussian character. These results suggest that a description of transport across sheared flows using effective diffusivities is oversimplified.

DOI: 10.1103/PhysRevLett.101.205002

PACS numbers: 52.35.Ra, 05.40.Fb, 52.55.Fa, 52.65.Tt

PHYSICS OF PLASMAS 16, 055905 (2009)

On the nature of radial transport across sheared zonal flows in electrostatic ion-temperature-gradient gyrokinetic tokamak plasma turbulence^{a)}

R. Sánchez,^{1,b)} D. E. Newman,² J.-N. Leboeuf,³ B. A. Carreras,⁴ and V. K. Decyk⁵ ¹Fusion Energy Division, Oak Ridge National Laboratory, Oak Ridge, Tennessee 37831-8071, USA ²Department of Physics, University of Alaska, Fairbanks, Alaska 99775-5920, USA ³JNL Scientific, Inc., Casa Grande, Arizona 85294-9695, USA ⁴BACV Solutions, Inc., Oak Ridge, Tennessee 37830-8222, USA ⁵UCLA, Los Angeles, California 90095-1547, USA

(Received 7 December 2008; accepted 15 April 2009; published online 7 May 2009)

It is argued that the usual understanding of the suppression of radial turbulent transport across a sheared zonal flow based on a reduction in effective transport coefficients is, by itself, incomplete. By means of toroidal gyrokinetic simulations of electrostatic, ion-temperature-gradient turbulence, it is found instead that the character of the radial transport is altered fundamentally by the presence of a sheared zonal flow, changing from diffusive to anticorrelated and subdiffusive. Furthermore, if the flows are self-consistently driven by the turbulence via the Reynolds stresses (in contrast to being induced externally), radial transport becomes non-Gaussian as well. These results warrant a reevaluation of the traditional description of radial transport across sheared flows in tokamaks via effective transport coefficients, suggesting that such description is oversimplified and poorly captures the underlying dynamics, which may in turn compromise its predictive capabilities. © 2009 American Institute of Physics. [DOI: 10.1063/1.3129727]

IOP PUBLISHING

PLASMA PHYSICS AND CONTROLLED FUSION

Plasma Phys. Control. Fusion 53 (2011) 074018 (10pp)

doi:10.1088/0741-3335/53/7/074018

Nature of turbulent transport across sheared zonal flows: insights from gyrokinetic simulations*

R Sanchez^{1,2}, D E Newman³, J-N Leboeuf⁴ and V K Decyk⁵

¹ Fusion Energy Division, Oak Ridge National Laboratory, Oak Ridge, TN 37831, USA

- ²Departamento de Física, Universidad Carlos III, Leganés 28911, Madrid, Spain
- ³ Department of Physics, University of Alaska, Fairbanks, AK 99775-5920, USA
- ⁴ JNL Scientific Inc., Casa Grande, AZ 85294-9695, USA

⁵ Department of Physics and Astronomy, University of California, Los Angeles, CA 90095-1547, USA

E-mail: sanchezferlr@ornl.gov and raul.sanchez@uc3m.es

Received 18 October 2010, in final form 28 February 2011 Published 18 May 2011 Online at stacks.iop.org/PPCF/53/074018

Abstract

The traditional view regarding the reduction of turbulence-induced transport across a stable sheared flow invokes a reduction of the characteristic length scale in the direction perpendicular to the flow as a result of the shearing and stretching of eddies caused by the differential pull exerted in the direction of the flow. A reduced effective transport coefficient then suffices to capture the reduction, that can then be readily incorporated into a transport model. However, recent evidence from gyrokinetic simulations of the toroidal iontemperature-gradient mode suggests that the dynamics of turbulent transport across sheared flows changes in a more fundamental manner, and that the use of reduced effective transport coefficients fails to capture the full dynamics that may exhibit both subdiffusion and non-Gaussian statistics. In this contribution, after briefly reviewing these results, we propose some candidates for the physical mechanisms responsible for endowing transport with such non-diffusive characteristics, backing these proposals with new numerical gyrokinetic data.



O<u>n-going</u> project: stellarators and quasi-symmetries @ BSC



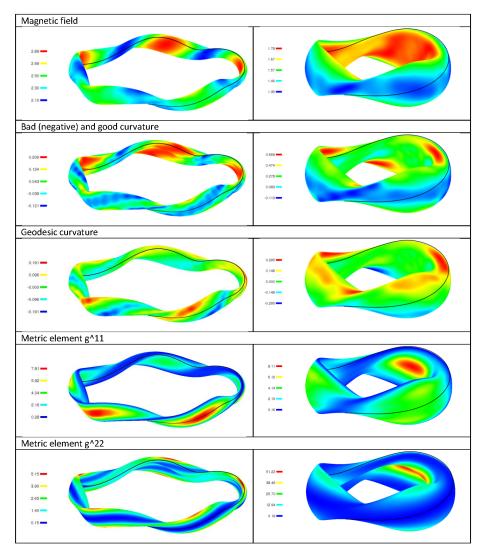
Stellarator design strategies are currently based on reducing neoclassical collisional transport by numerically looking for quasi-symmetries of the confining magnetic field.

Quasi-symmetries are hidden symmetries of the magnitude of the magnetic field when written in Boozer coordinates. These are non-geometrical coordinates, so QS configurations do not look symmetric to the naked eye.

Turbulent transport has been theorized to improve in QS configurations, mostly due to the reduced neoclassical viscosities that should allow for the self-consistent generation of poloidal flows.

On-going project tries to determine the nature of transport as a function of the degree of QS of the configuration.

IPP's GENE/GIST code is used, since it can handle a general 3D geometry.





- Ministerio de Economía y Competitividad, España.
- Department of Energy, Office of Fusion Science, USA.
- Arctic Region Supercomputing Center (University of Fairbanks, Alaska, USA)
- Barcelona Supercomputer Center (Red Española de Supercomputación)
- National Energy Research Supercomputing Center (Lawrence Livermore Natl. Lab, California, USA)
- Universidad Carlos III de Madrid, SPAIN
- University of Alaska at Fairbanks, USA
- Oak Ridge National Laboratory, Tennessee, USA
- University of California at Los Angeles, USA
- Institut-für-Plasmaphysik, Max Planck Institüt, Greifswald, GERMANY