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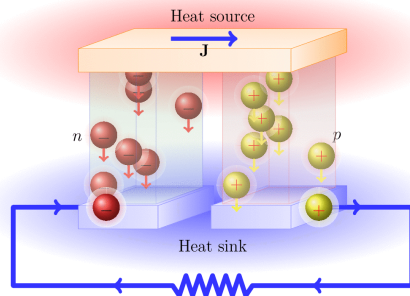
# THERMAL TRANSPORT IN DISORDERED NANOSTRUCTURED MATERIALS

*5th HPC Advisory Council Spain Conference & 10th RES Users 'Conference  
León (Spain), September 20, 2016*

## Manipulating heat flow at the nanoscale

### THERMOELECTRIC DEVICES

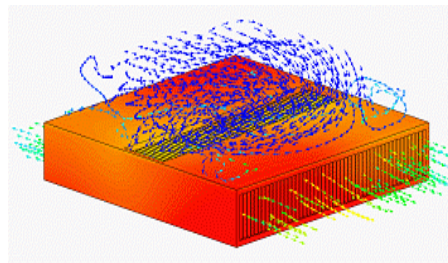
Conversion of  $\Delta T$  into electricity through the Seebeck effect



$$ZT = S^2 T \frac{\sigma}{\kappa}$$

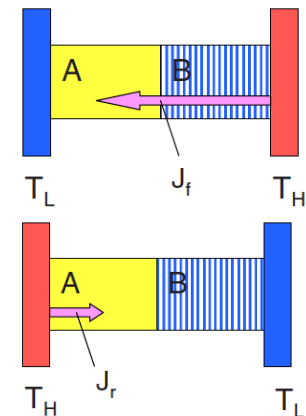
### THERMAL MANAGEMENT

Heat dissipation at the nanoscale is becoming a major issue



New generation electron devices must be cooled

### PHONONICS

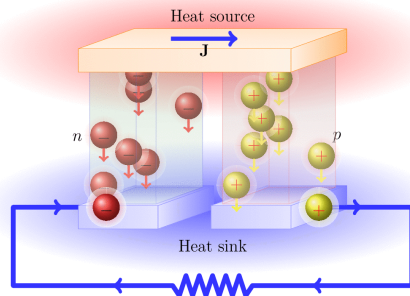


Manipulating heat flow to code and transmit information

## Manipulating heat flow at the nanoscale

### THERMOELECTRIC DEVICES

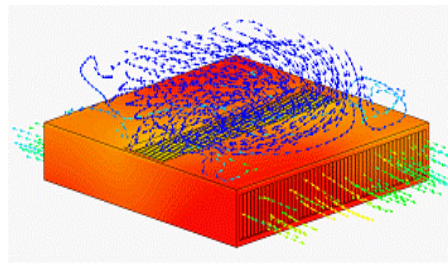
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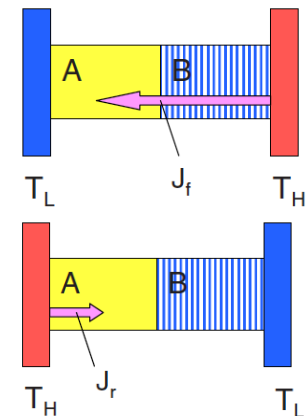
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Manipulating heat flow to code and transmit information

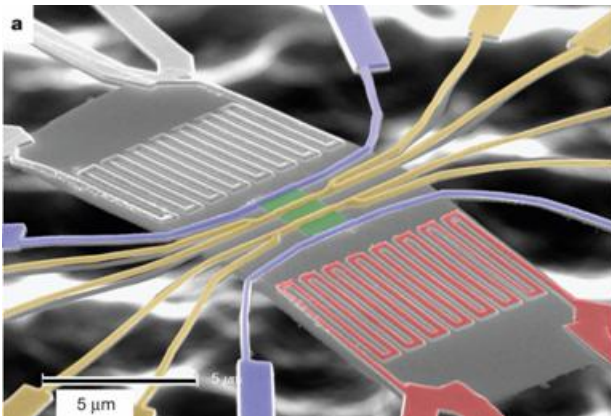


$$ZT = S^2 T \frac{\sigma}{\kappa}$$

electrical  
conductivity

thermal  
conductivity

## Thermoelectrics



Boukai *et al.*, Nature **451**, 168 (2008)

How do we increase  $ZT$ ?

Either increasing the electrical conductivity or decreasing the thermal conductivity

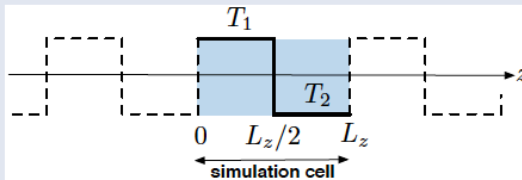


## ① Molecular dynamics

- Si-Ge interactions modelled by the **Tersoff potential**
- use of **large-scale simulation cells** (up to  $\mathcal{O}(10^6)$  atoms)
- LAMMPS code

## ② Non-equilibrium simulations

- **approach-to-equilibrium-MD**  
*Melis et al., EPJ-B 87, 96 (2014)*



- average local temperature:  
$$T_{i,ave}(t) = \frac{1}{L_z/2} \int_0^{L_z/2} T(z;t) dz$$
- time-dependent temperature offset:  
$$\Delta T(t) = T_{1,ave}(t) - T_{2,ave}(t)$$
- fit  $\kappa$  on

$$\Delta T(t) = \sum_{n=1}^{\infty} C_n e^{-\alpha_n^2 \kappa t / \rho C_V}$$

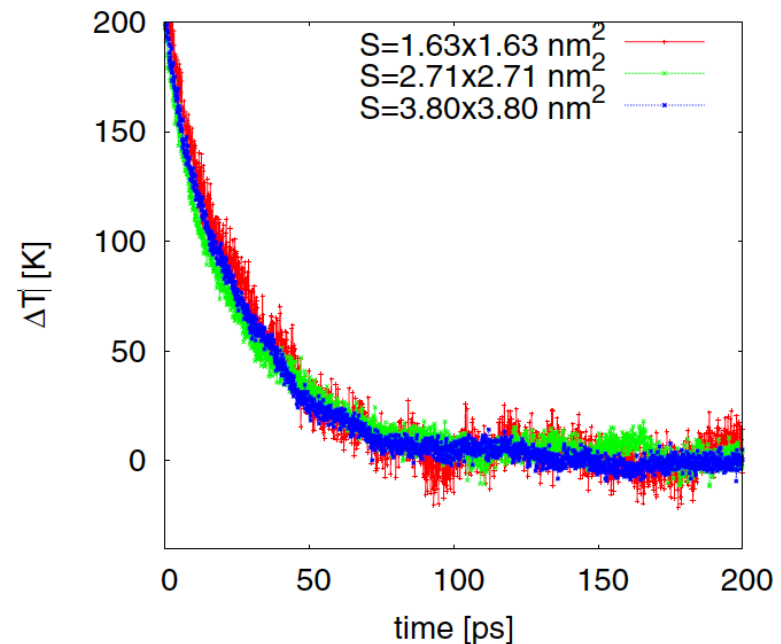
$\Delta T(t)$  calculated on-the-fly in the AEMD run

FI-2014-1-0001/0003

*Nanoporous silicon for thermoelectric applications*

FI-2016-1-0022

*Thermal transport in isotopically disordered Si NWs*

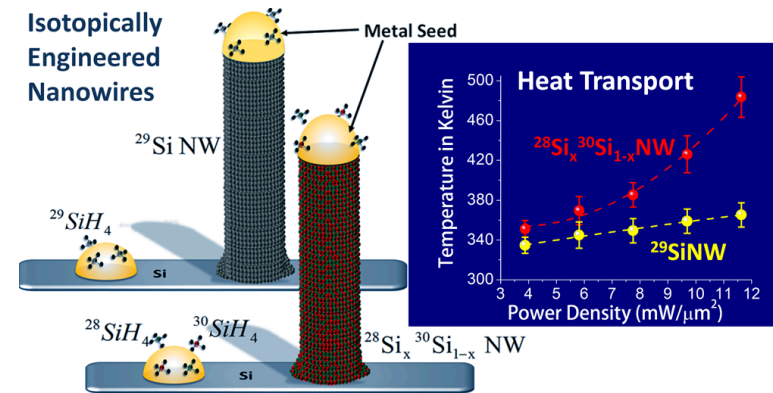


*Melis et al., Eur. Phys. J. B 87, 96 (2014)*

Tuning thermal  
transport in Si NWs by  
isotope engineering

# Isotope engineering in Si NWs

**Isotope blends** represent a textbook approach to increase the ZT in a semiconductor



Mukherjee *et al.*, Nano Lett. **15**, 3885 (2015)

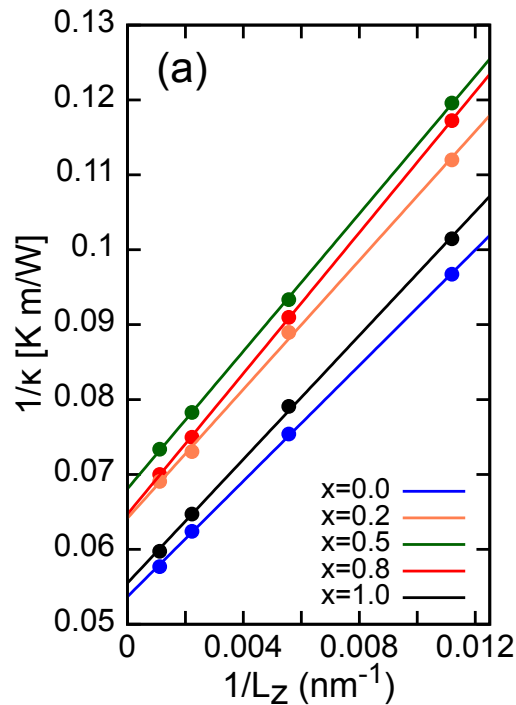
Isotopes have different masses, but the same electron shell configuration. Therefore, the electrical conductivity,  $\sigma$  is preserved, while—as by adding different isotopes one is adding scattering centres for the incoming phonons— $\kappa$  will decrease, leading to the corresponding increase of ZT.

We study heat transport in  $^{28}\text{Si}_x^{30}\text{Si}_{1-x}$  NWs as a function of the composition  $x$  and account for the nonuniform radial distribution observed in the experiments of Mukherjee and coworkers.



# Isotope engineering in Si NWs

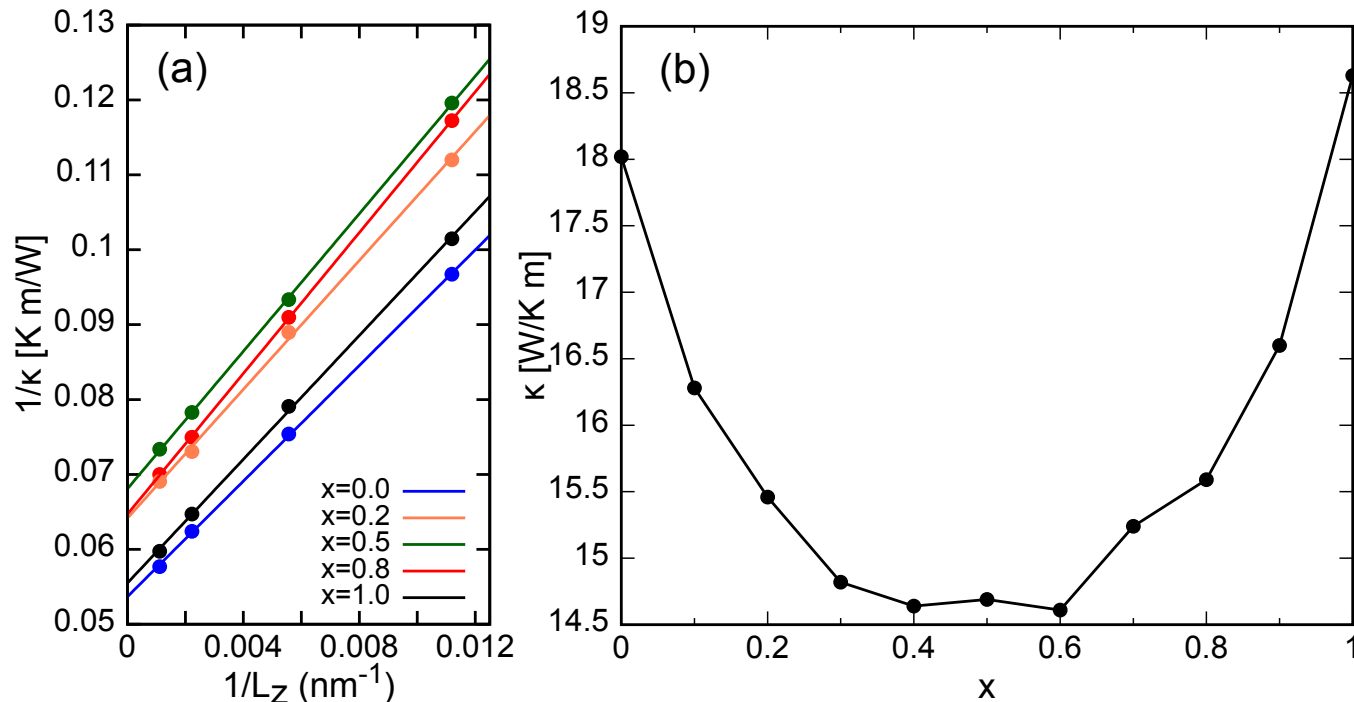
$^{28}\text{Si}_{1-x}^{30}\text{Si}_x$  NWs, 15 nm diameter



To get rid of finite size effect one must calculate  $\kappa$  for increasing cell sizes and extrapolate its value in the  $\kappa^{-1}=\kappa^{-1}(L_z^{-1})$  plot for  $L_z^{-1} \rightarrow 0$  (i.e.  $L_z \rightarrow \infty$ )

# Isotope engineering in Si NWs

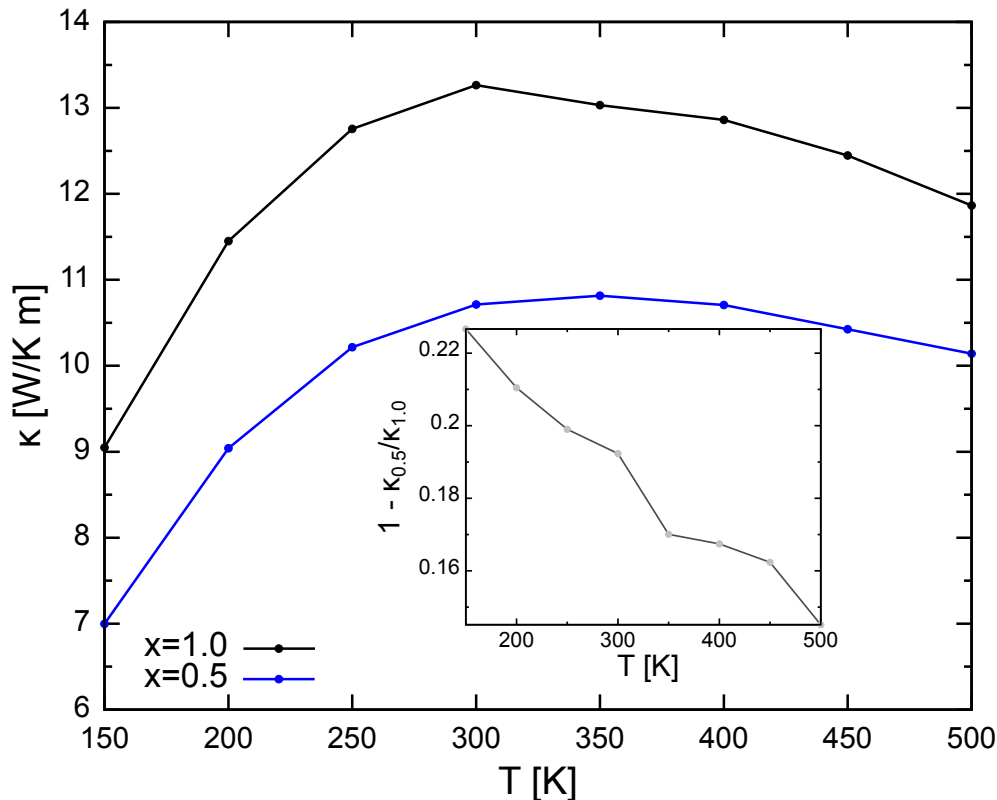
$^{28}\text{Si}_{1-x}^{30}\text{Si}_x$  NWs, 15 nm diameter



We obtain a U-shape curve similar to previously reported data of  $\text{Si}_{1-x}\text{Ge}_x$  alloys  $\Rightarrow$  a precise control of the composition is not required to achieve the maximum reduction of  $\kappa$ , around 20% with respect to isotope purified NWs

# Isotope engineering in Si NWs

$^{28}\text{Si}_{0.5}^{30}\text{Si}_{0.5}$  NWs, 15 nm diameter

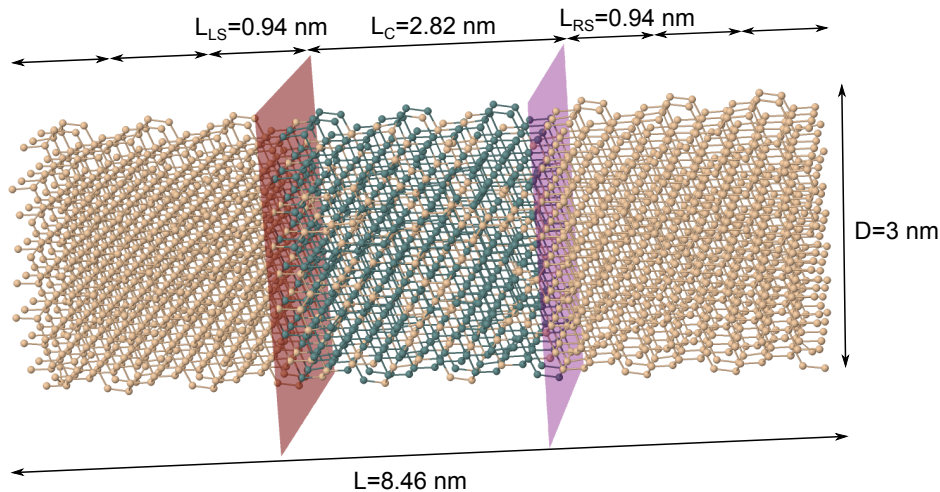


At **high temperature** isotopes are somewhat **less efficient** to reduce the thermal conductivity

This observation suggests that it's worth while giving a look at the (very) low temperature regime, but there MD results are not reliable because of quantum effects

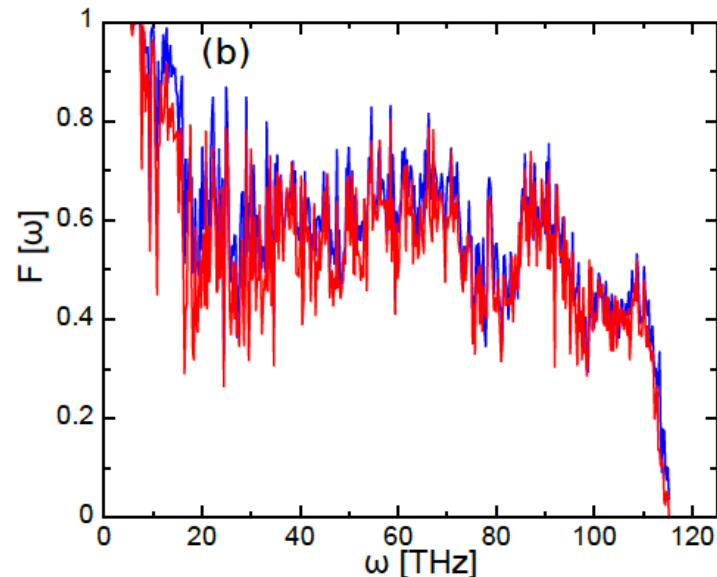
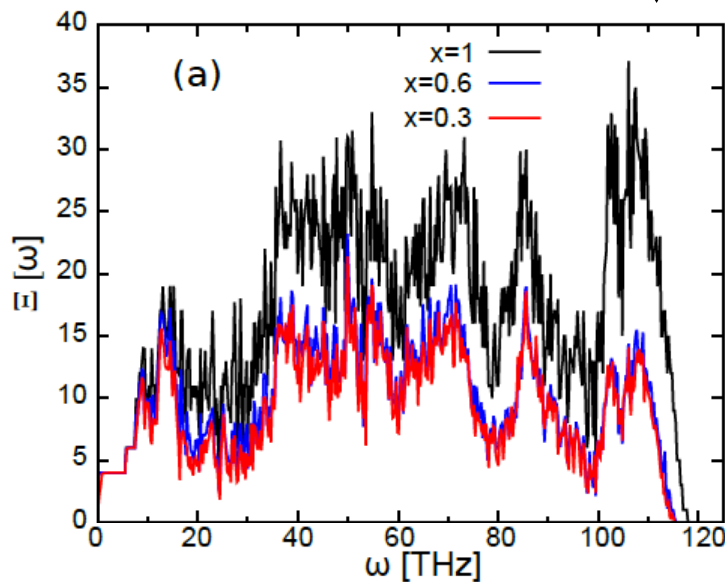


# Isotope engineering in Si NWs



We tackle the low temperature limit within **nonequilibrium Green's functions**

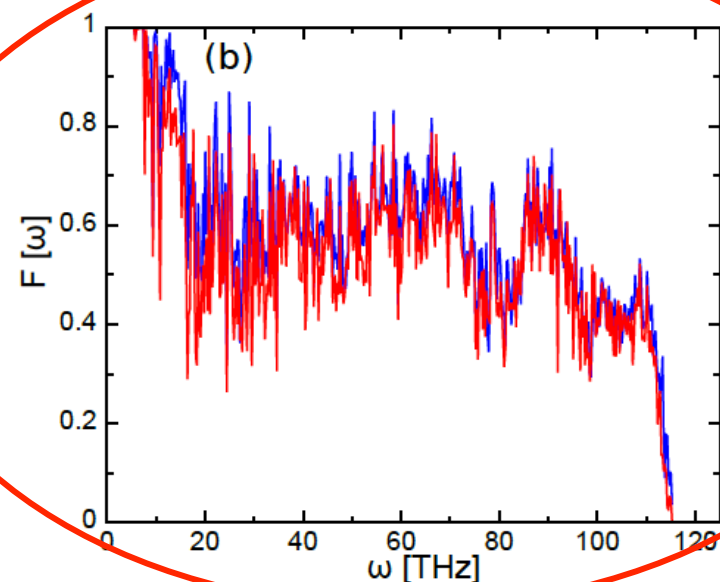
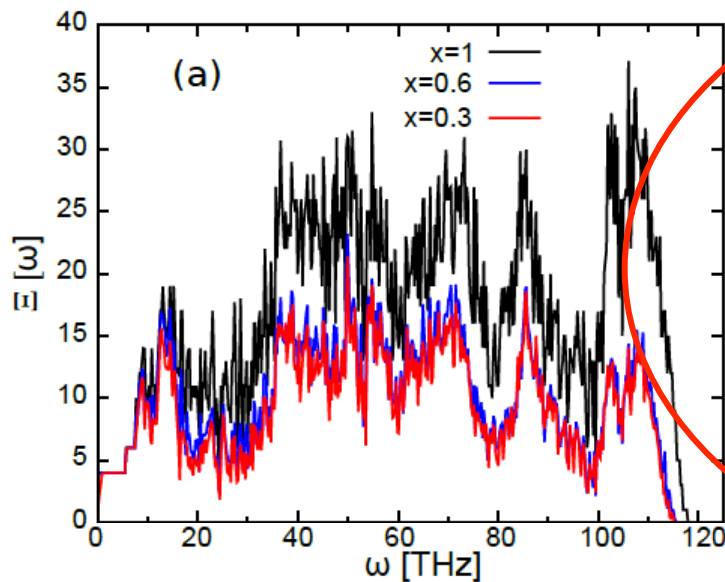
The conductance in harmonic approximation is calculated as the transmission probability of scattering states



# Isotope engineering in Si NWs

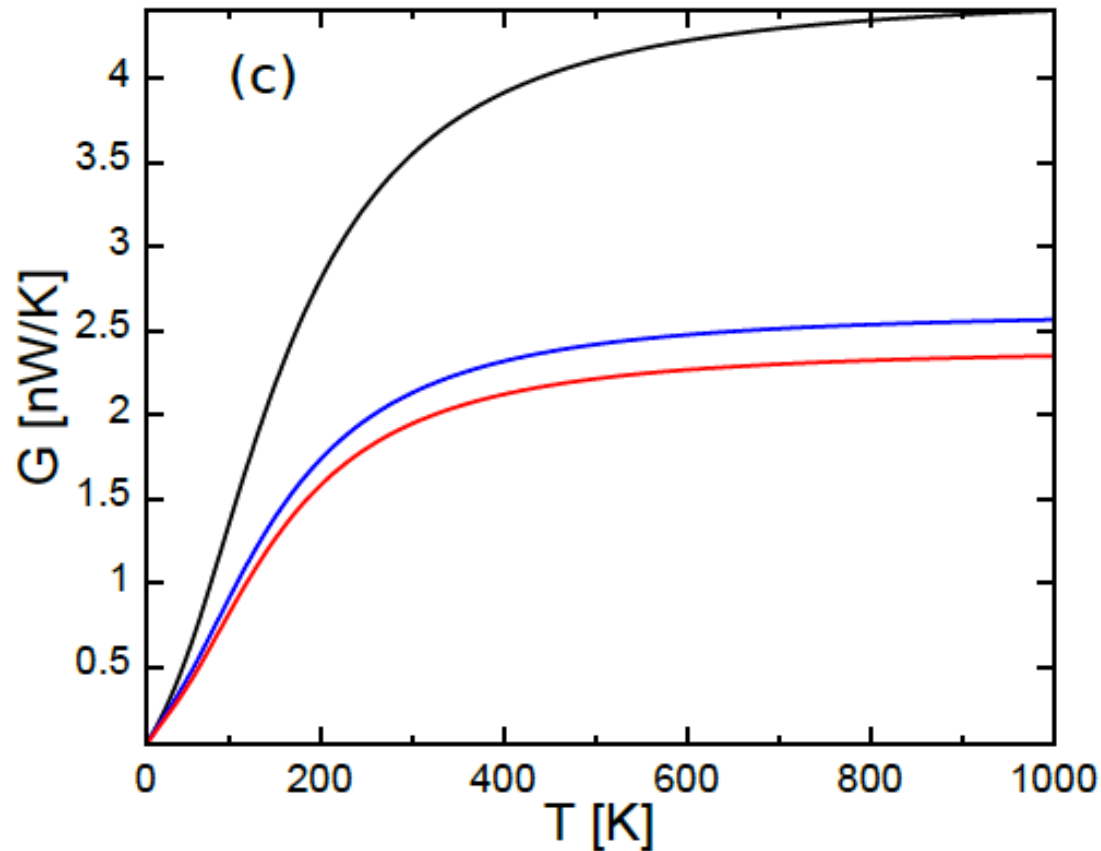
A substitutional isotope defect does not distort the host lattice, thus scattering mostly comes from short wavelength phonons

These results suggest that isotope engineering can be used to implement a **phonon low-pass filter** that mostly suppress midrange and high phonon frequencies



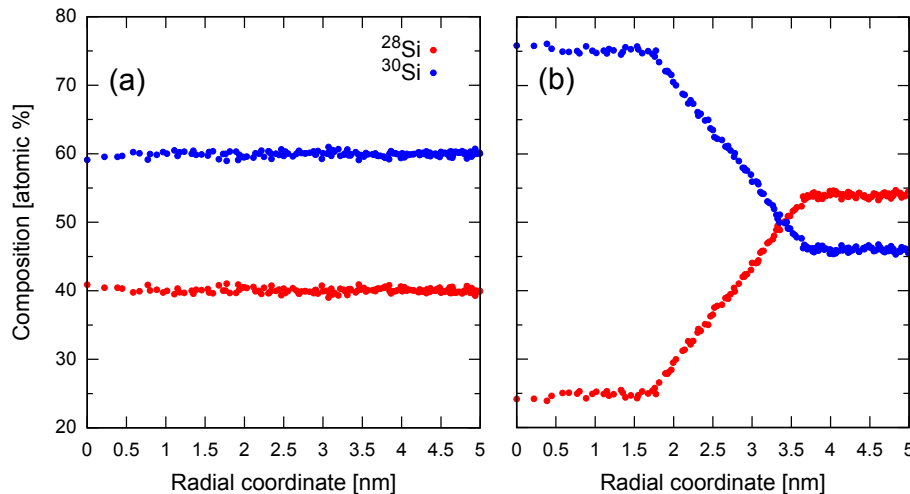
# Isotope engineering in Si NWs

As hinted by the high temperature MD results, in the very low temperature regime, **reductions of  $\kappa$  of up to the 50% can be achieved**





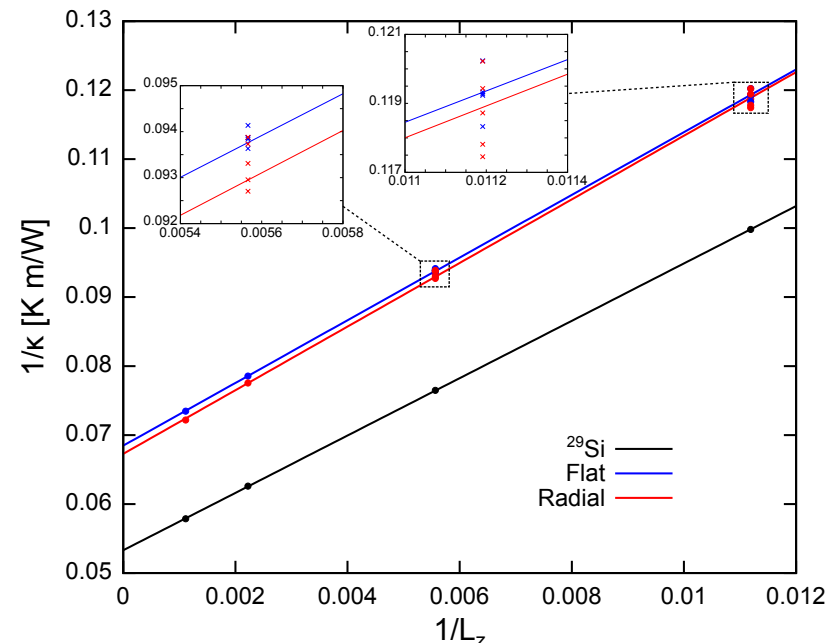
# Isotope engineering in Si NWs



Finally, we compared **different radial profiles** for a  $^{28}\text{Si}_{0.4}^{30}\text{Si}_{0.6}$  NW: (left) A uniform distribution and (right) Accumulation of heavy isotopes in the wire core as observed experimentally

We did **not** detect a sizeable difference between the two cases

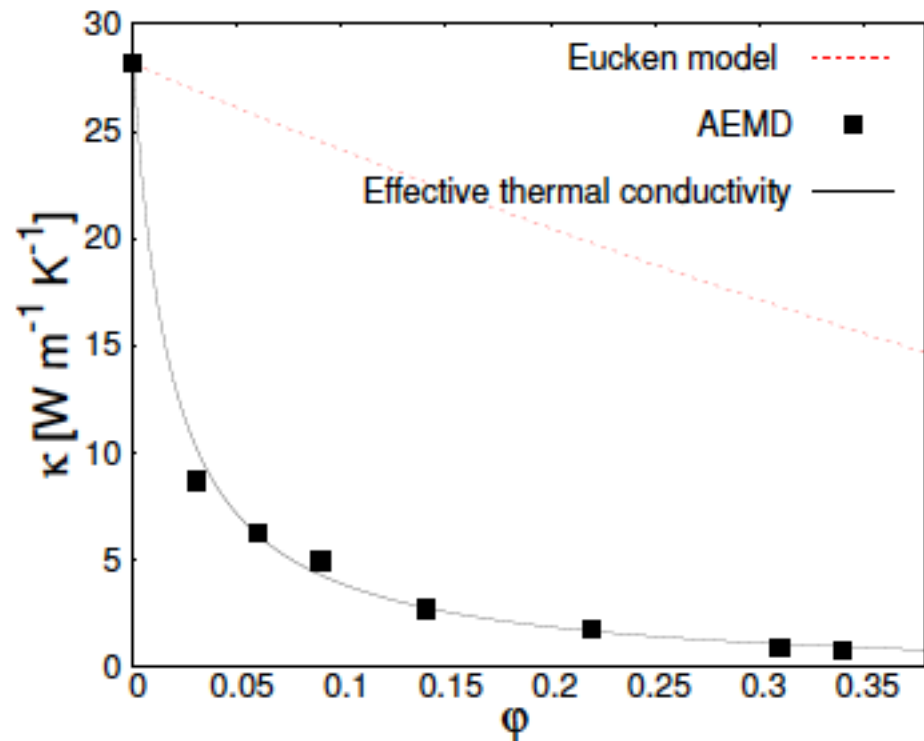
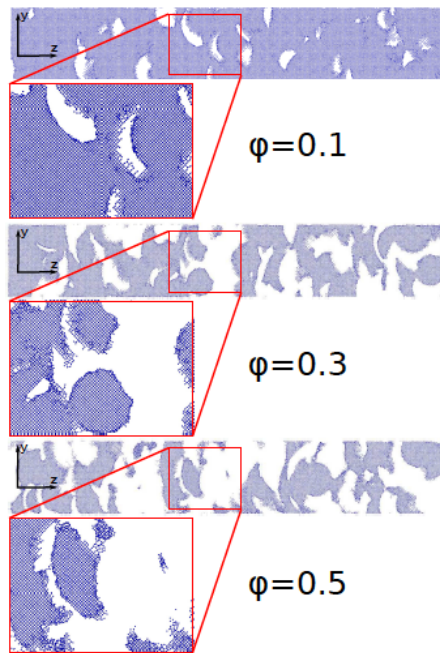
This results is not unexpected. The non-uniform radial profile studied can be seen as **a coaxial structure** with a  $^{28}\text{Si}_{0.25}^{30}\text{Si}_{0.75}$  core and a  $^{28}\text{Si}_{0.55}^{30}\text{Si}_{0.45}$  shell and we have shown that a  $^{28}\text{Si}_x^{30}\text{Si}_{1-x}$  NWs with  $x=0.25$  and  $x = 0.55$  have roughly the same  $\kappa$



# Thermal transport in porous Si NWs

It has been shown that the thermal conductivity can be reduced by

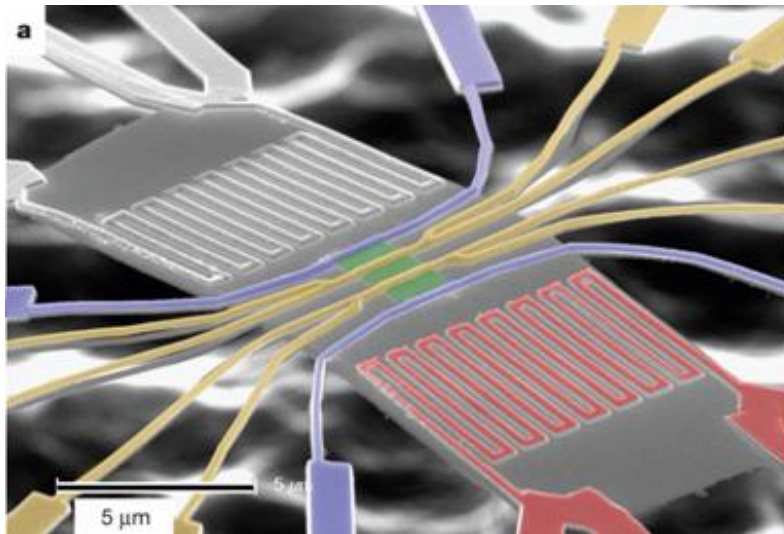
- (i) nanopores in a bulk material
- (ii) surface scattering in nanowires



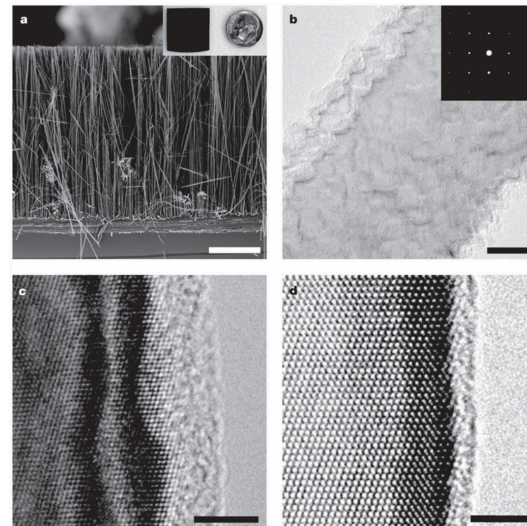


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Hochbaum *et al.*, Nature **451**, 163 (2008)



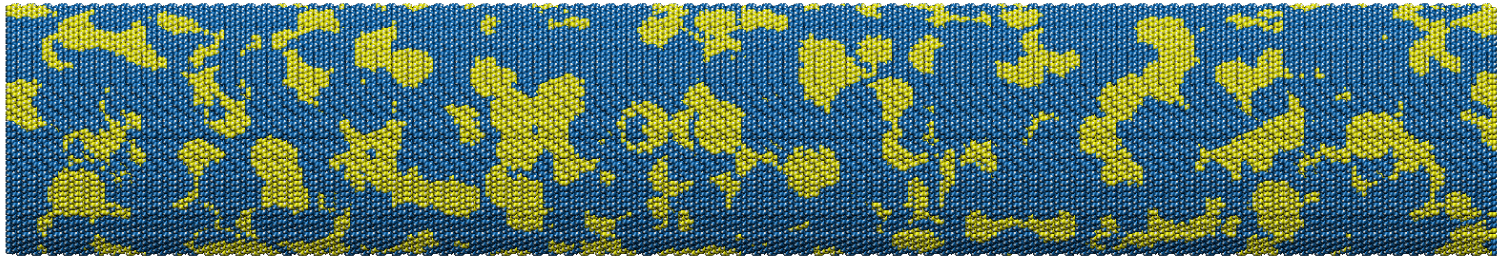
Boukai *et al.*, Nature **451**, 168 (2008)

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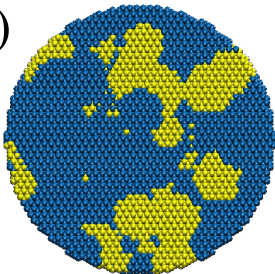
- (i) nanopores in a bulk material
- (ii) surface scattering in nanowires

Why not bringing these two features together: **porous Si nanowires**

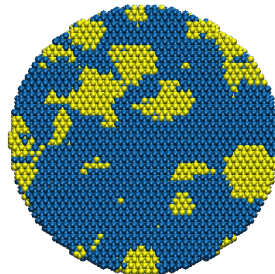
(a)



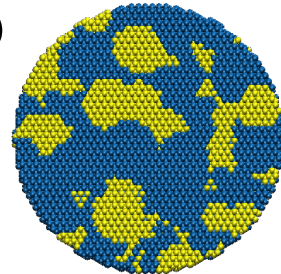
(b)



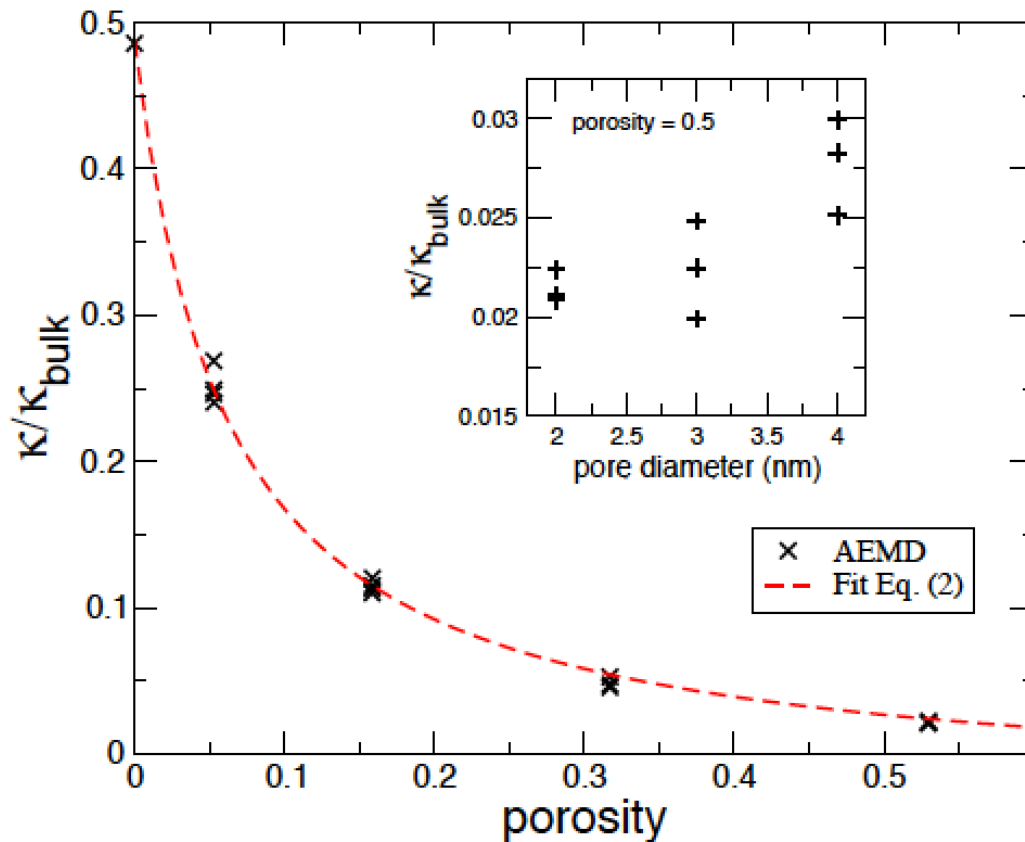
(c)



(d)



# Porous Si NWs



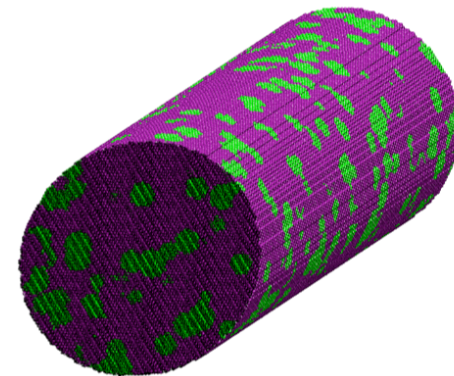
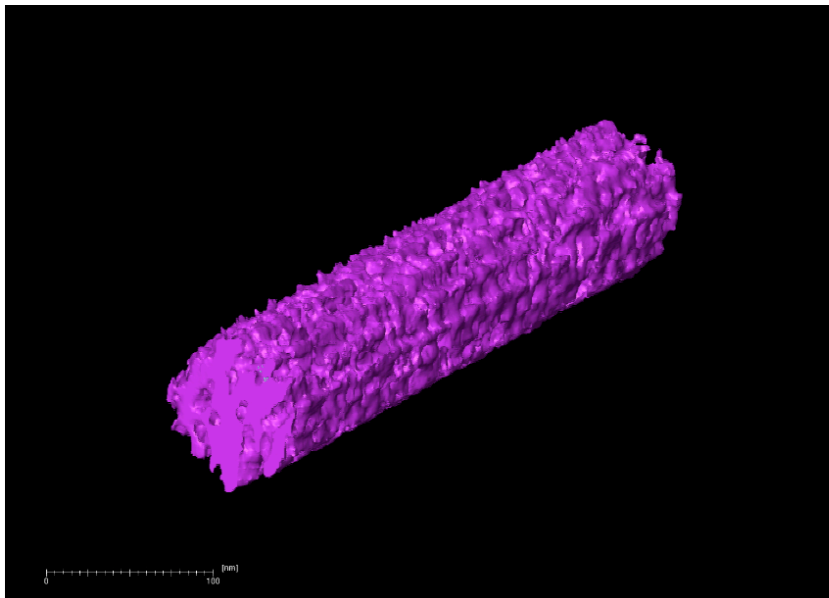
15 nm diameter SiNWs; pores of 3 nm

- Boundary scattering alone accounts for a reduction of a factor of two for the pristine ( $\phi=0$ ) NW with respect to bulk
- A rather low porosity  $\phi=0.3$  results in an additional reduction of one order of magnitude ( $\kappa/\kappa_{\text{bulk}} \sim 0.05$ )
- We set up a predictive model, which provides an excellent agreement with the MD results

$$\frac{\kappa}{\kappa_{\text{bulk}}} = \frac{1 - \phi}{1 + \frac{\phi}{2} + \frac{3\phi}{2d_p} \Lambda_{\text{bulk}} + \frac{\beta}{d_{\text{NW}}} \Lambda_{\text{bulk}}}$$

# Porous Si NWs

pSi NWs electrical conductivity is, at least in principle, tunable by gas doping, thus their ZT could be not-so-bad...



**Talos200X STEM tomography at 200kV**

Image size:	2kx2k	Frame time:	22 s
Tilt range:	-67° — 78°	Tilt step:	1°

**Talos200X STEM tomography at 200kV**

Image size:	708x2048x495	Binning:	1
Method:	SIRT		

## Acknowledgements





Want to know more???

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SOME READING...:

These works

- M. Royo and R. Rurali, Phys. Chem. Chem. Phys. (2016), doi:10.1039/C6CP04581B
- X. Cartoixa, R. Dettori, C. Melis, L. Colombo, and R. Rurali, Appl. Phys. Lett. **109**, 013107 (2016)

Review papers on NWs

- R. Rurali, Rev. Mod. Phys. **82**, 427 (2010)
- M. Amato, M. Palummo, R. Rurali, and S. Ossicini, Chem. Rev. **114**, 1371 (2014)
- M. Amato and R. Rurali, Progr. Surf. Sci. **91**, 1 (2016)

Thank you for your attention!

Whenever anyone says, 'theoretically' they really mean, 'not really'  
Dave Parnas